

## SHOCK ABSORBERS

Four parameters are required to precisely determine the dimension of shock absorbers:

- Mass to be decelerated  $m$  (kg)
- Impact velocity  $v$  (m/s)
- Propelling or driving force  $F$  (N)
- Number of impact cycles per hour  $C$  (/hr)

Some useful calculation formulas:

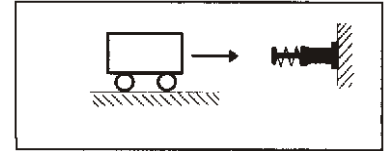
- Kinetic energy:  $E_k = mv^2/2$
- Drive energy:  $E_d = F \cdot S$
- Free fall velocity:  $v = \sqrt{2g \cdot h}$
- Pneumatic or hydraulic cylinder driving forces:  
 $F = 0.00785 Pd^2$
- Maximum shock force (approximate):  
 $F_m = 1.2 E_T/S$
- Propelling force generated by electric motors:  
 $F = 3000 \text{ kW}/v$
- Total energy absorbed per hour:  
 $E_{TC} = E_T \cdot C$

Symbols	Unit	Description
$\mu$		Coefficient of friction
$\alpha$	(rad)	Angle of incline
$\theta$	(rad)	Side load angle
$\omega$	(rad/s)	Angular velocity
$A$	(m)	Width
$B$	(m)	Thickness
$C$	(/hr)	Impact cycles per hour
$d$	(mm)	Cylinder bore diameter
$E_d$	(Nm)	Drive energy per cycle
$E_k$	(Nm)	Kinetic energy per cycle
$E_T$	(Nm)	Total energy per cycle
$E_{TC}$	(Nm)	Total energy per hour
$F$	(N)	Propelling force
$F_m$	(N)	Maximum shock force
$g$	(m/s <sup>2</sup> )	Acceleration due to gravity (9.81 m/s <sup>2</sup> )
$h$	(m)	Height
HM		Arresting torque factor for motors (normally 2.5)
kW	(kW)	Electric motor power
$m$	(kg)	Mass to be decelerated
$M_m$	(kg)	Effective mass
$P$	(bar)	Operation pressure
$R_s$	(m)	Radius
$R$	(m)	Shock absorber mounting distance from rotation center
$S$	(m)	Stroke
$T$	(Nm)	Driving torque
$t$	(s)	Deceleration time
$v$	(m/s)	Velocity of impact mass
$v_s$	(m/s)	Impact velocity at shock absorber

### Example 1: Horizontal impact

Application data:

$m = 300\text{kg}$   
 $v = 1.0\text{m/s}$   
 $S = 0.04\text{m}$   
 $C = 300/\text{hr}$



Formulas and calculation:

$$E_k = \frac{mv^2}{2} = \frac{300 \cdot 1.0^2}{2} = 150\text{Nm}$$

$$E_T = E_k = 150\text{Nm}$$

$$E_{TC} = E_T \cdot C = 150 \cdot 300 = 45000\text{Nm/hr}$$

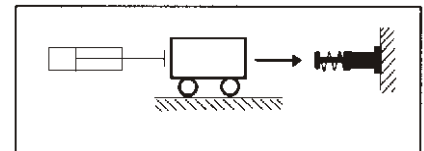
$$M_e = \frac{2E_T}{v^2} = \frac{2 \cdot 150}{1.0^2} = 300\text{kg}$$

Choose from sizing diagram: MAD3650 is adequate

### Example 2: Horizontal impact with propelling force

Application data:

$m = 300\text{kg}$   
 $v = 1.2\text{m/s}$   
 $S = 0.05\text{m}$   
 $P = 40\text{N/cm}^2$   
 $d = 100\text{mm}$   
 $C = 300/\text{hr}$



Formulas and calculation:

$$E_k = \frac{mv^2}{2} = \frac{300 \cdot 1.2^2}{2} = 216\text{Nm}$$

$$E_d = F \cdot S = 0.00785 Pd^2 \cdot S$$

$$= 0.00785 \cdot 40 \cdot 100^2 \cdot 0.05 = 157\text{Nm}$$

$$E_T = E_k + E_d = 216 + 157 = 373\text{Nm}$$

$$E_{TC} = E_T \cdot C = 373 \cdot 300 = 111900\text{Nm/hr}$$

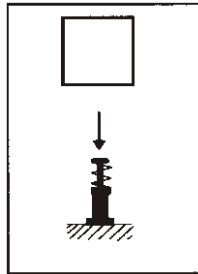
$$M_e = \frac{2E_T}{v^2} = \frac{2 \cdot 373}{1.2^2} = 518\text{kg}$$

Choose from sizing diagram: MAD4250 is adequate

### Example 3: Free fall impact

**Application data:**

m = 40kg  
h = 0.4m  
S = 0.06m  
C = 200/hr



**Formulas and calculation:**

$$v = \sqrt{2g \cdot h} = \sqrt{2 \cdot 9.81 \cdot 0.4} = 2.8\text{m/sec}$$

$$E_k = \frac{mv^2}{2} = \frac{40 \cdot 2.8^2}{2} = 157\text{Nm}$$

$$E_d = F \cdot S = mg \cdot h = 40 \cdot 9.81 \cdot 0.06 = 23.5\text{Nm}$$

$$E_T = E_k + E_d = 157 + 23.5 = 180.5\text{Nm/hr}$$

$$E_{TC} = E_T \cdot C = 180.5 \cdot 200 = 36100\text{Nm/hr}$$

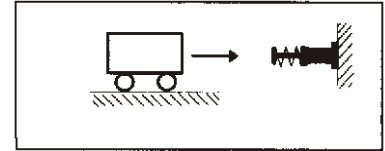
$$M_e = \frac{2E_T}{V^2} = \frac{2 \cdot 180.5}{2.8^2} = 46\text{kg}$$

Choose from sizing diagram: MAC3660-1 is adequate

### Example 5: Horizontal impact with motor driving

**Application data:**

m = 400kg  
v = 1.0m/s  
kW = 1.5kW  
HM = 2.5  
S = 0.075m  
C = 60/hr



**Formulas and calculation:**

$$E_k = \frac{mv^2}{2} = \frac{400 \cdot 1.0^2}{2} = 200\text{Nm}$$

$$E_d = F \cdot S = \frac{\text{kW} \cdot \text{HM}}{v} \cdot S = \frac{1500 \cdot 2.5}{1.0} \cdot 0.075 = 281\text{Nm}$$

$$E_T = E_k + E_d = 200 + 281 = 481\text{Nm}$$

$$E_{TC} = E_T \cdot C = 481 \cdot 60 = 25860\text{Nm/hr}$$

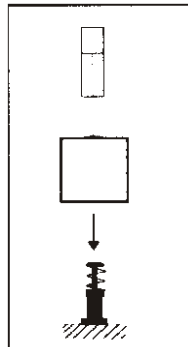
$$M_e = \frac{2E_T}{V^2} = \frac{2 \cdot 481}{1.0^2} = 962\text{kg}$$

Choose from sizing diagram: MAD4275 is adequate

### Example 4: Free fall impact with propelling

**Application data:**

m = 40kg  
h = 0.3m  
S = 0.025m  
P = 5bar  
d = 50mm  
C = 200/hr  
v = 1.0m/sec



**Formulas and calculation:**

$$E_k = \frac{mv^2}{2} = \frac{40 \cdot 1.0^2}{2} = 20\text{Nm}$$

$$E_d = F \cdot S = (mg + 0.0785Pd^2) \cdot S = (40 \cdot 9.81 + 0.0785 \cdot 5 \cdot 50^2) \cdot 0.025 = 33.5\text{Nm}$$

$$E_T = E_k + E_d = 20 + 33.5 = 55.5\text{Nm}$$

$$E_{TC} = E_T \cdot C = 55.5 \cdot 200 = 11100\text{Nm/hr}$$

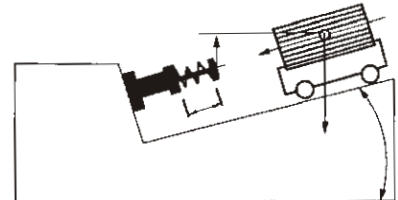
$$M_e = \frac{2E_T}{V^2} = \frac{2 \cdot 55.5}{1.0^2} = 111\text{kg}$$

Choose from sizing diagram: MAD2525 is adequate

### Example 6: Inclined impact

**Application data:**

m = 150kg  
h = 0.3m  
S = 0.075m  
 $\alpha = 30^\circ$   
C = 200/hr



**Formulas and calculation:**

$$v = \sqrt{2g \cdot h} = \sqrt{2 \cdot 9.81 \cdot 0.3} = 2.43\text{m/sec}$$

$$E_k = \frac{mv^2}{2} = \frac{150 \cdot 2.43^2}{2} = 443\text{Nm}$$

$$E_d = F \cdot S = m \cdot g \cdot S \cdot \sin \alpha = 150 \cdot 9.81 \cdot 0.075 \cdot \sin 30^\circ = 55.2\text{Nm}$$

$$E_T = E_k + E_d = 443 + 55.2 = 498.2\text{Nm/hr}$$

$$E_{TC} = E_T \cdot C = 498.2 \cdot 200 = 99640\text{Nm/hr}$$

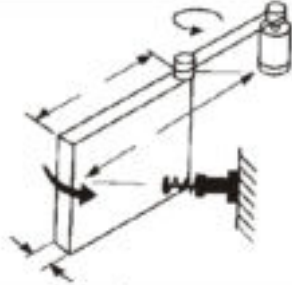
$$M_e = \frac{2E_T}{V^2} = \frac{2 \cdot 498.2}{2.43^2} = 168.7\text{kg}$$

Choose from sizing diagram: MAD4275 is adequate

### Example 7: Horizontal rotating door

**Application data:**

$m = 20\text{kg}$   
 $\omega = 2.0\text{rad/s}$   
 $T = 20\text{Nm}$   
 $R_s = 0.8\text{m}$   
 $A = 1.0\text{m}$   
 $B = 0.05\text{m}$   
 $S = 0.016\text{m}$   
 $C = 100/\text{hr}$



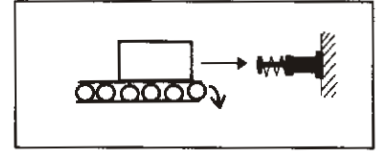
$I$	$= \frac{m(4A^2+B^2)}{12}$	$= \frac{20(4 \cdot 1.0^2+0.05^2)}{12}$	$= 6.67\text{kg} \cdot \text{m}^2$
$E_k$	$= \frac{I\omega^2}{2}$	$= \frac{6.67 \cdot 2.0^2}{2}$	$= 13.34\text{Nm}$
$\theta$	$= \frac{s}{R_s}$	$= \frac{0.04}{0.8}$	$= 0.05\text{rad}$
$E_b$	$= T \cdot \theta$	$= 20 \cdot 0.05$	$= 1.0\text{Nm}$
$E_T$	$= E_k + E_b$	$= 13.34 + 1.0$	$= 14.34\text{Nm}$
$E_{TC}$	$= E_T \cdot C$	$= 14.34 \cdot 100$	$= 1434\text{Nm/hr}$
$v$	$= \omega \cdot R_s$	$= 2.0 \cdot 0.8$	$= 1.6\text{m/s}$
$M_e$	$= \frac{2E_T}{V^2}$	$= \frac{2 \cdot 14.34}{1.6^2}$	$= 11.20\text{kg}$

Choose from sizing diagram: MAD2016 is adequate

### Example 9: Horizontal mass on driven rollers

**Application data:**

$m = 150\text{kg}$   
 $v = 0.5\text{m/s}$   
 $\mu = 0.25$   
 $S = 0.02\text{m}$   
 $C = 120/\text{hr}$



**Formulas and calculation:**

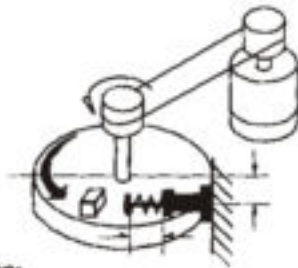
$E_k$	$= \frac{mv^2}{2}$	$= \frac{150 \cdot 0.5^2}{2}$	$= 18.75\text{Nm}$
$E_b$	$= F \cdot S = mg\mu \cdot S$	$= 150 \cdot 9.81 \cdot 0.25 \cdot 0.02$	$= 7.35\text{Nm}$
$E_T$	$= E_k + E_b$	$= 18.75 + 7.35$	$= 26.1\text{Nm}$
$E_{TC}$	$= E_T \cdot C$	$= 26.1 \cdot 120$	$= 3132\text{Nm/hr}$
$M_e$	$= \frac{2E_T}{V^2}$	$= \frac{2 \cdot 26.1}{0.5^2}$	$= 208.8\text{kg}$

Choose from sizing diagram: MAC2020-3 is adequate

### Example 8: Rotary index table with propelling force

**Application data:**

$m = 200\text{kg}$   
 $\omega = 1.0\text{rad/s}$   
 $T = 100\text{Nm}$   
 $R = 0.5\text{m}$   
 $R_s = 0.4\text{m}$   
 $S = 0.04\text{m}$   
 $C = 100/\text{hr}$



**Formulas and calculation:**

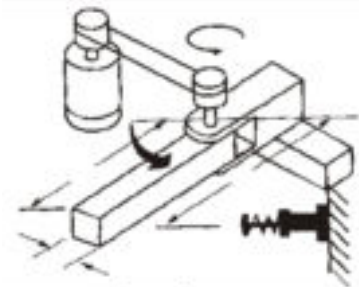
$I$	$= \frac{mR^2}{2}$	$= \frac{200 \cdot 0.5^2}{2}$	$= 25\text{kg} \cdot \text{m}^2$
$E_k$	$= \frac{I\omega^2}{2}$	$= \frac{25 \cdot 1.0^2}{2}$	$= 12.5\text{Nm}$
$\theta$	$= \frac{s}{R_s}$	$= \frac{0.04}{0.4}$	$= 0.1\text{rad}$
$E_b$	$= T \cdot \theta$	$= 100 \cdot 0.1$	$= 10\text{Nm}$
$E_T$	$= E_k + E_b$	$= 12.5 + 10$	$= 22.5\text{Nm}$
$E_{TC}$	$= E_T \cdot C$	$= 22.5 \cdot 50$	$= 1125\text{Nm/hr}$
$v$	$= \omega \cdot R_s$	$= 1.0 \cdot 0.4$	$= 0.4\text{m/s}$
$M_e$	$= \frac{2E_T}{V^2}$	$= \frac{2 \cdot 22.5}{0.4^2}$	$= 281\text{kg}$

Choose from sizing diagram: MAD2540 is adequate

### Example 10: Rotating beam with driving force

**Application data:**

$m = 40\text{kg}$   
 $A = 0.5\text{m}$   
 $B = 0.05\text{m}$   
 $\omega = 2.0\text{rad/s}$   
 $T = 10\text{Nm}$   
 $R_s = 0.4\text{m}$   
 $S = 0.05\text{m}$   
 $C = 50/\text{hr}$



$I$	$= \frac{m(4A^2+B^2)}{12}$	$= \frac{40(4 \cdot 0.5^2+0.05^2)}{12}$	$= 3.36\text{kg} \cdot \text{m}^2$
$E_k$	$= \frac{I\omega^2}{2}$	$= \frac{3.36 \cdot 2.0^2}{2}$	$= 6.8\text{Nm}$
$\theta$	$= \frac{s}{R_s}$	$= \frac{0.05}{0.4}$	$= 0.125\text{rad}$
$E_b$	$= T \cdot \theta$	$= 10 \cdot 0.125$	$= 1.25\text{Nm}$
$E_T$	$= E_k + E_b$	$= 6.8 + 1.25$	$= 8.05\text{Nm}$
$E_{TC}$	$= E_T \cdot C$	$= 8.05 \cdot 50$	$= 402.5\text{Nm/hr}$
$v$	$= \omega \cdot R_s$	$= 2.0 \cdot 0.4$	$= 0.8\text{m/s}$
$M_e$	$= \frac{2E_T}{V^2}$	$= \frac{2 \cdot 8.05}{0.8^2}$	$= 25.15\text{kg}$

Choose from sizing diagram: MAD1416-2 is adequate